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First-Principles Theoretical Study on Electronic Band Structure of Diamond and Graphite

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Authors' contributions

This work was carried out in collaboration between all authors. Author MAA designed the study, performed the statistical analysis, wrote the protocol, and wrote the first draft of the manuscript. Authors SGA and MYO managed the analyses of the study. Author MAA managed the literature searches. All authors read and approved the final manuscript.

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Original Research Article

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ABSTRACT

The total ground state energy and electronic band structure of Graphite and Diamond were calculated in this work using FHI-aims (Fritz Haber Institute ab initio molecular simulations) Density Functional Theory (DFT) code. The density functionals used are the generalised gradient functional PBE, and PBE+vdW approach as defined by Tkatchenko and Scheffler. The results obtained from the computations of the ground state energies of diamond and graphite were -2056.898408114 eV and -2061.703700984 eV respectively. Similarly, the results obtained from the calculations of the electronic band gaps of graphite and diamond were 0.0 eV and 5.56369215 eV, respectively. These are in good agreement when compared to the experimental values of 0eV and 5.48eV. These band gaps are within reasonable percentage errors of 0.0% and 1.46% respectively. This shows that DFT has overestimated the band gap of diamond by 0.08 eV in our computations.

Keywords: DFT; diamond; electronic band structure; DOS and graphite.

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1. INTRODUCTION

For many years the band structure emerging from density functional theory was the only electronic structure free of experimental parameters that could be calculated to interpret carrier levels, doping, chemical bonding, etc. As such, it still has enormous reach in the community as a Baseline against which better (formally more rigorous) approximations are compared [1]. The electronic band structures of graphite and diamond are particularly critical because of their unique semiconducting applications and fascinating properties. Researchers have studied the band structure of pure hexagonal graphite using nonlocal ionic pseudopotential [2], compared the band structure and DOS of the three graphite structures using an ab initio norm-conserving pseudopotential [3].

On the other hand, an empirical pseudopotential method was used [4] to calculate the band structure of diamond. In 1970, [5] also computed the band structure of diamond using nonlocal pseudopotential method. Similarly, the band gap of diamond was calculated by [6] using both LDA and GGA functionals. The methods mentioned above involved an empirical and pseudopotential computations, an all-electron/full Potential with the numeric atom-centred basis function computational method is therefore necessary to study the band structure of these new Carbon allotropes. In this work, the electronic band structure of diamond and graphite were simulated using FHI-aims DFT package [7]. This paper aims to re-investigate the ground state electronic properties as well as predict the suitable potential electronic applications of diamond and graphite.

2. MATERIALS AND METHODS

First-principles calculations continue to be a successful method of electronic structure calculations. Starting with the fundamental constants and Schrödinger's equation as a postulate, these methods proceed to describe the nature of atomistic systems to the degree that is almost irrefutable. The methods applied in solving Schrodinger's equation break into two main types: Hartree-Fock (HF) based methods and Density Functional Theory (DFT) methods. While both make approximations possible, calculations to make they represent the best available methods for atomistic modelling.

The original idea of DFT (i.e. using the electron density) is dated back to the individual work of [8,9]. In Thomas-Fermi model, they showed that the distribution of electrons in an atom is uniform and can be approximated using statistical considerations. In 1964, [10] proved two essential but straightforward theorems, which later become the basis of DFT. In 1965, in trade of simplicity for accuracy, [11] invented an ingenious indirect approach to the theory in such a way that the kinetic energy can be computed merely to reasonable accuracy, leaving a small residual correction that is handled separately. They showed that one could build a theory using simpler formulas also referred to as Kohn-Sham (KS) kinetic energy functional and ground state electron density, namely;

$$T_{s}[n] = \langle \psi_{i} | -\frac{1}{2} \nabla_{i}^{2} | \psi_{i} \rangle$$
(1.1)

and

$$n(\vec{r}) = \sum_{i=S}^{N} \left| \psi_{i}(\vec{r}S) \right|^{2}$$
(1.2)

Where ψ_{i} are the original spin orbitals? To give a unique value to the KS kinetic energy functional $T_{s}[n]$ through Eq. (1.1), KS invoked a corresponding non-interacting reference system, with the Hamiltonian:

$$\hat{H}_{s} = \sum_{i}^{N} \left(-\frac{1}{2} \nabla_{i}^{2} \right) + \sum_{i}^{N} V_{s}(\vec{r})$$
(1.3)

In which there are no electron-electron repulsion terms, and for which the ground state electron density is precisely $n(\vec{r})$. KS thus established that for any real (interacting) system with ground state density $n(\vec{r})$, there always exists a non-interacting system with the same ground state density $n(\vec{r})$ For this system there will be an exact determinantal ground state wave function;

$$\Psi_{S} = \frac{1}{\sqrt{N!}} \det \left[\Psi, \Psi, \dots, \Psi \right].$$
(1.4)

where ψ_i are the *N* lowest eigenstates of the one-electron Hamiltonian $\stackrel{\scriptscriptstyle\wedge}{H}_{e}$

$$\stackrel{\wedge}{H}_{s} \boldsymbol{\psi}_{i} = \left[\left(-\frac{1}{2} \nabla_{i}^{2}\right) + V_{s}(\vec{r})\right] \boldsymbol{\psi}_{i} = \boldsymbol{\varepsilon}_{i} \boldsymbol{\psi}_{i} \quad (1.5)$$

Now, to produce $T_{s}[n]$ precisely as the kinetic energy component [12] of T[n] in HK theorem, KS reformulate the universal functional as;

$$F[n] = \frac{1}{s}[n] + J[n] + E_{xc}[n]$$
(1.6)

where;

$$E_{xc}[n] = T[n] - \prod_{S} [n] + V[n] - J[n]$$
(1.7)

The defined quantity E_{xc} [*n*] is called the exchange-correlation energy functional. The corresponding Euler equation for Eq. (1.7) is;

$$\mu = V_{eff} \left(\stackrel{\rightarrow}{r} \right) + \frac{\delta T_s[n]}{\delta n \left[\stackrel{\rightarrow}{r} \right]}$$
(1.8)

Where $V_{e\!f\!f}(\vec{r})$ is the KS effective potential and is defined by;

$$V_{eff}(\vec{r}) = V_{ne}(\vec{r}) + \frac{\delta J[n]}{\delta n[r]} + \frac{\delta E_{xc}[n]}{\delta n[r]}$$
(1.9)

$$V(\vec{r}) = V_{ne}(\vec{r}) + \int \frac{n[\vec{r}]}{|\vec{r} - \vec{r}|} d\vec{r} + V(\vec{r})$$
(2.0)

The second term of Eq. (2.0) is the Hartree potential while the XC potential $V_{xc}(\vec{r})$ is given as

$$V_{xc}(\vec{r}) = \frac{\delta E_{xc}[n]}{\vec{\delta n[r]}}$$
(2.1)

Therefore, for a given $V(\vec{r})$, one gets the $n(\vec{r})$ simply by solving the *N* one-electron equations;

$$[(-\frac{1}{2}\nabla_{i}^{2}) + \underset{eff}{V}(\vec{r})]\psi_{i} = \varepsilon_{i}\psi_{i} \qquad (2.2)$$

and setting

$$n(\vec{r}) = \sum_{i}^{N} \sum_{S} |\psi_{i}(\vec{r}S)|^{2}$$
(2.3)

The productive potential from Eq. (1.9) Depends on the electron density; therefore the Kohn-Sham equations have to be solved self-consistently. The electronic total energy *E* is typically calculated using the sum over the Kohn-Sham eigenvalues;

$$E = \sum_{i}^{N} \varepsilon_{i} - \frac{1}{2} \iint \frac{n \begin{pmatrix} \overrightarrow{r} \\ 1 \end{pmatrix} n \begin{pmatrix} \overrightarrow{r} \\ 2 \end{pmatrix}}{| \stackrel{\overrightarrow{r} \rightarrow \overrightarrow{r} }{| \stackrel{\overrightarrow{r} \rightarrow \overrightarrow{r} }}}}}$$
(2.4)

The Kohn-Sham scheme is in principle exact. The approximation only enters when we have to decide on an explicit form for the unknown functional for the exchange-correlation energy $E_{xc}[n]$ and its corresponding potential $V_{xc}(\stackrel{\rightarrow}{r})$. The main goal of modern DFT is therefore to find better approximations to these two functionals. A great variety of different approximations $V(\vec{r})$ have been developed. For many years the local density approximation (LDA) has been used [13]. In LDA, the exchange-correlation energy density at a point in space is taken to be that of the homogeneous electron gas with the local electron density. Thus the total exchange-correlation energy functional is approximated as,

$$E_{xc}^{LDA} = \int \vec{n(r)} \mathcal{E}_{xc}(\vec{n(r)}) d\vec{r}$$
^(2.5)

.

From which the potential is obtained using Eq. 2.1. However, LDA can have significant errors in its approximations some physical and chemical for properties computations. Recently, an effective potential that depend both on the local density and the magnitude of its local gradient are widely used. They are known as generalized gradient approximations functionals. The (GGA) GGA's total exchange-correlation energy functional is approximated as,

$$E_{xc}^{GGA}[n_{\uparrow,}n_{\downarrow}] = \int_{\mathcal{E}_{xc}} (n_{\uparrow,}n_{\downarrow,} \vec{\nabla}n_{\uparrow} \vec{\nabla}n_{\downarrow}) n(\vec{r}) d\vec{r}$$
(2.6)

There are many GGA versions among which is the Perdew Burke Ernzerhof (be) functional (1997) used in this study. On the other hand, there are many DFT computational codes among which is the FHI-aims package. FHI-aims is a computer program package for computational materials science based only on quantummechanical first principles mathematical model. It uses solution methods of DFT to compute the total energy and derived guantities of molecular or solid condensed matter in its electronic ground state (Blum et al, 2009). In addition, FHI-aims describing a wave-function based allow molecular total energy calculation based on Hartree-Fock and many-body perturbation theory (MP2 and MP4).

2.1 Computational Details

Total ground state energy of graphite and diamond were calculated in the Generalized Gradient Approximation (GGA) and Local Density Approximation (LDA) using the [14] and [15], exchange-correlation energy functionals respectively. The calculation was performed by

using Brillouin-zone of 12×12×12 k-point grids for the SCF convergence. For the interplanar lattice parameter c of graphite, vdW effects correction based on [16] was included into the PBE functional. In order to generate a smooth-looking DOS, we used a denser 8×8×8 k-space grid to integrate the DOS for diamond. The factors by which the original k-space grid from the SCF cycle is increased are now (8, 8, 8). Together with the original k-grid of 12×12×12, this makes for a 96×96×96 integration mesh that is used for the DOS. However, we used a less dense 5×5×5 k-space grid to integrate the DOS for graphite. A Gaussian broadening of 0.05eV was used for both structures DOS computations. We used an experimental lattice constant of a = 3.567 Å and a = 2.461 Å, c = 6.708Å for diamond and graphite respectively. Fig. 1 shows crystalline structures that were used for computational simulations. In (Fig. 1a), diamond crystalline lattice is presented. For graphite (Fig. 1b), graphene sheets are shown, however a unit cell of the bulk graphite structure was used for this work.

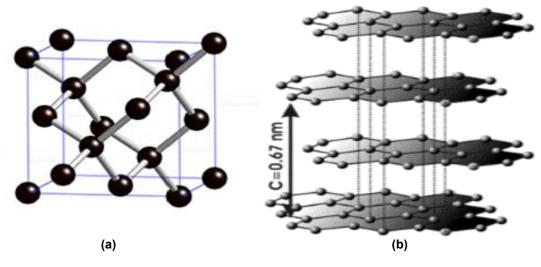


Fig. 1. Structures Simulated (a) Diamond (b) Graphite

3. RESULTS

The following table summarises the output data obtained during FHI-aims computations,

Bands structure	Lowest unoccupied state (eV)	Highest occupied country (eV)	Energy difference (eV)
Diamond	-2.66537760	-8.22906975	5.56369215

Table 1. Band gaps for diamond

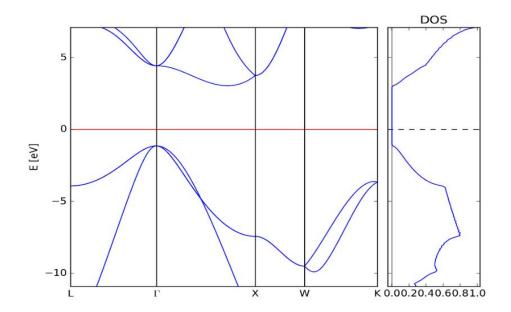


Fig. 2. Band Structure and Density of States of the bulk Diamond as generated by the 'aimsplot.py.' script

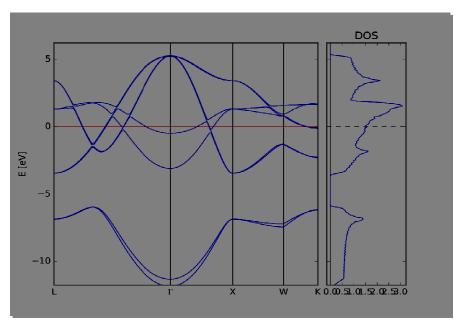


Fig. 3. Band Structure and Density of States of the bulk Graphite as generated by the 'aimsplot.py.' script

4. DISCUSSION

Figs. 2 and 3 show the band structures and DOS for diamond and graphite respectively. The zero shows the position of the Fermi level in the band structure of these crystals on the energy scale, and vertical lines indicate that of symmetry points on the band graph in Fig. 2 and Fig. 3.

In Fig. 2, there is an essential characteristic of the band structure, namely the range of energies where there are no electronic states across the entire Brillouin zone; this is the band gap. The Fermi level within the band gap shows that all state below it remains occupied and all state above remain unoccupied. From the plot and shown in Table 1 the energy difference between the lowest empty land and the highest occupied country along reciprocal space direction number one is 5.56369215 eV. This value differs from other theoretical and experimental values by 0.12 eV and 0.08 eV, respectively [6,17]. Since the valence band maximum at **F**-point and the conduction band minimum partially at X - the point is on different symmetry point, it shows that diamond is an indirect band gap semiconductor with a significant energy gap value of 5.56 eV. The similar result of an indirect bandgap semiconductor for AIAs and diamond were also computed using FHI-aims code [18,19]. The DOS for the unit cell in Fig 2 also shows that the number of the electronic states in the valence bands is more than that of the conduction bands.

In Fig. 3, there is another important characteristic of the band structure, namely a narrow or zero gap range of energies where there are no electronic states; the Figure shows that graphite does not have a gap because there is an overlap between the valence and conduction bands. This zero-gap value agrees with other theoretical and experimental work [3,20]. It is obvious that the Fermi level lies within the conduction band, this shows that the conduction band is partially filled. The bands can be seen to touch at the entire L-K region of the Brillouin zone. The overlapping points on the Fermi level is between π nonbonding orbitals in different graphite planes. This is simply because, in graphite the strong bonding between the segments connecting nearest-neighbour atoms within the layers (intralayer) is described by sp^2 hybridized 2s, $2p_x$, and $2p_v$ atomic orbitals (σ -states), and the weak interlayer bonding is derived from the overlap between $2p_z$ orbitals (π -states) perpendicular to the graphitic planes. The resulting band structure consists of bonding π and $\sigma\text{-states}$ and antibonding π * and σ * states forming the valence and conduction bands, respectively. The weak interactions between graphitic planes is such that these bands split which leads to a zero-gap semiconductor and create a wide overlap semimetal [3,17,21]. The splitting of the bands at the Fermi level is in agreement with experiment [2]. As the electronic nature of a structure depends on the density of states in the region of the Fermi level, the theoretical overlap three regions of peaks are presented in the DOS of Fig. 3.

5. CONCLUSION

The total ground state energy and electronic band structure of Graphite for hcp and Diamond crystal were calculated using the LDA in the parameterization by Perdew and Zunger 1981, the generalized gradient functional PBE, and PBE+vdW approach as defined by Tkatchenko and Scheffler. The results of the total energy required for binding/stability of the ground state during the optimized process were found to converge faster with the 12x12x12 k-grid points in the Brillouin zone of the FHI-aims code. We have found that a DFT LDA/GGA calculation of diamond and graphite electronic band structure and DOS gives correct location and shape of the Fermi level, band gap, VBM and CBM. The comparison between theory and experiment is better than could have been expected from bandgap studies with similar formalism.

COMPETING INTERESTS

Authors have declared that no competing interests exist.

REFERENCES

- Ruiz V, Blum V. Theoretical material science: Electronic structure theory at the computer. Exercise Sheet 9: Electron band structure and density of states. Based on an exercise by Juergen Wieferink, Lydia Nemec, and Volker Blum, Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin; 2012.
- Charlier Gonze JCX, Michenaud JP. Firstprinciples study of the electronic properties of graphite. Physical Review B. 1991;43(6): 4579-4589.
- Charlier Gonze JCX, Michenaud JP. Firstprinciples study of the stacking effect on the electronic properties of graphite(s). Carbon. 1994;32(2):289-299.
- Saslow W, Bergstresser TK, Cohen ML. Band structure and optical properties of diamond. Physical Review Letters. 1966;16(9):354-356.
- Louis A, Hamstreeet Jr, Fong CY, Cohen ML. Calculation of the band structure and optical constants of diamond using the nonlocal-pseudopotential method. Physical Review B. 1970;2(6):2054-2063.
- Belenkov EA, Brzhezinskaya MM, Greshnyakov VA. Crystalline structure and properties of diamond-like materials. Nanosystems: Physics, Chemistry, Mathematics. 2017;8(1):127-136. DOI: 10.17586/22208054201781127136.
- Blum V, Gehrke R, Hanke F, Havu P, Havu V, Ren X, Reuter K, Matthias S. Ab Initio molecular simulations with numeric atom-

centered orbitals. Computer Physics Communication. 2009;180(11):2175–2196.

- Thomas LH. The calculation of atomic Fields. In Mathematical Proceedings of the Cambridge Philosophical Society. 1927;23: 542-548. [Reprinted in March 1975].
- 9. Fermi, E. Un metodo statistice per la determinazione di alcune proprieta dell'atomo. Rend Accad. 1927;6:602-607. (French).
- Hohenberg P, Kohn W. Inhomogeneous Electron Gas. Phys. Rev. 1964;136(3B): B864–B871.
- Kohn W, Sham LJ. Self-consistent equations including exchange and correlation effects. Phys. Rev. 1965;140 (4A):A1133–A1138. Available:<u>http://dx.doi.org/10.1103/physRe</u> v.140.A1133
- 12. Parr RG, Yang W. Density-functional theory of atoms and molecules. Oxford University Press: New York; 1989.
- Abdu SG, Babaji G. DFT calculations of the lattice constant, stable atomic Structure and the ground state total energy of silicon. Journal of the Nigerian Association of Mathematical Physics. 2013;24(1):89-92.
- Perdew JP, Burke K, Ernzerhof M. Generalized gradient approximation made simple. Phys. Rev. Letter. 1997;77(18): 3865–3868.
- 15. Perdew JP, Zunger A. Self-interaction correction to density-functional

approximations for many-electron systems. Physical Review B. 1981;23:5048-5079. Available:<u>http://dx.doi.org/10.1103/PhysRe</u> vB.23.5048.

- Tkatchenko A, Scheffler M. Accurate molecular van der Waals interactions from ground state electron density and freeatom reference data. Physical Review Letters. 2009;102(7):073005.
 DOI: 10.1103/PhysRevLett.102.073005.
- 17. Pierson HO. Handbook of carbon, graphite, diamond and fullerenes. Noyes Publications, New Mexico; 1993.
- Owolabi JA, Onimisi MY, Abdu SG, 18. Olowomofes GO. Determination of band gallium-arsenide structure of and aluminium-arsenide using density functional theory. Computational Chemistry. 2016;4:73-82. Available:http://dx.doi.org/10.4236/cc.2016 .43007
- Abdu SG, Adamu MA, Onimisi MY. Energetics of the basic allotropes of carbon. 2018;18(1). (In Press).
- 20. Krueger A. Carbon materials and nanotechnology. WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim; 2010.
- 21. Newton Ooi, Asit Rairkar, James Adams B. Density functional study of graphite bulk and surface properties. Carbon. 2006;44: 231–242.

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